




Mathematics Policy

Smawthorne Henry Moore Academy
Accomplish Multi-Academy Trust



Policy Name	Mathematics Policy	
Policy Owner	Accomplish MAT	
Version Reference	Version 1	
Approved by	SHMA Local Governing Board	
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Review Date	November 2026	

Calculations Policy

At the centre of the mastery approach to the teaching of mathematics is the belief that all pupils have the potential to succeed. Children should all have access to their age-appropriate curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling varied and challenging problems. Similarly with calculation strategies, pupils must not simply rote learn procedures but demonstrate their understanding of these principles and concepts through the use of concrete materials and pictorial representations to ensure fluency and depth of understanding.

The rationale of the concrete-pictorial-abstract (CPA) approach is that for pupils to have a true understanding of a mathematical concept, they need to master all three phases. Reinforcement is achieved by going back and forth between these representations. Pupils who grasp concepts rapidly should be challenged through rich and sophisticated problems before any acceleration through new content. Those pupils who are not sufficiently fluent with earlier material should consolidate their understanding, including additional practice, before moving on.

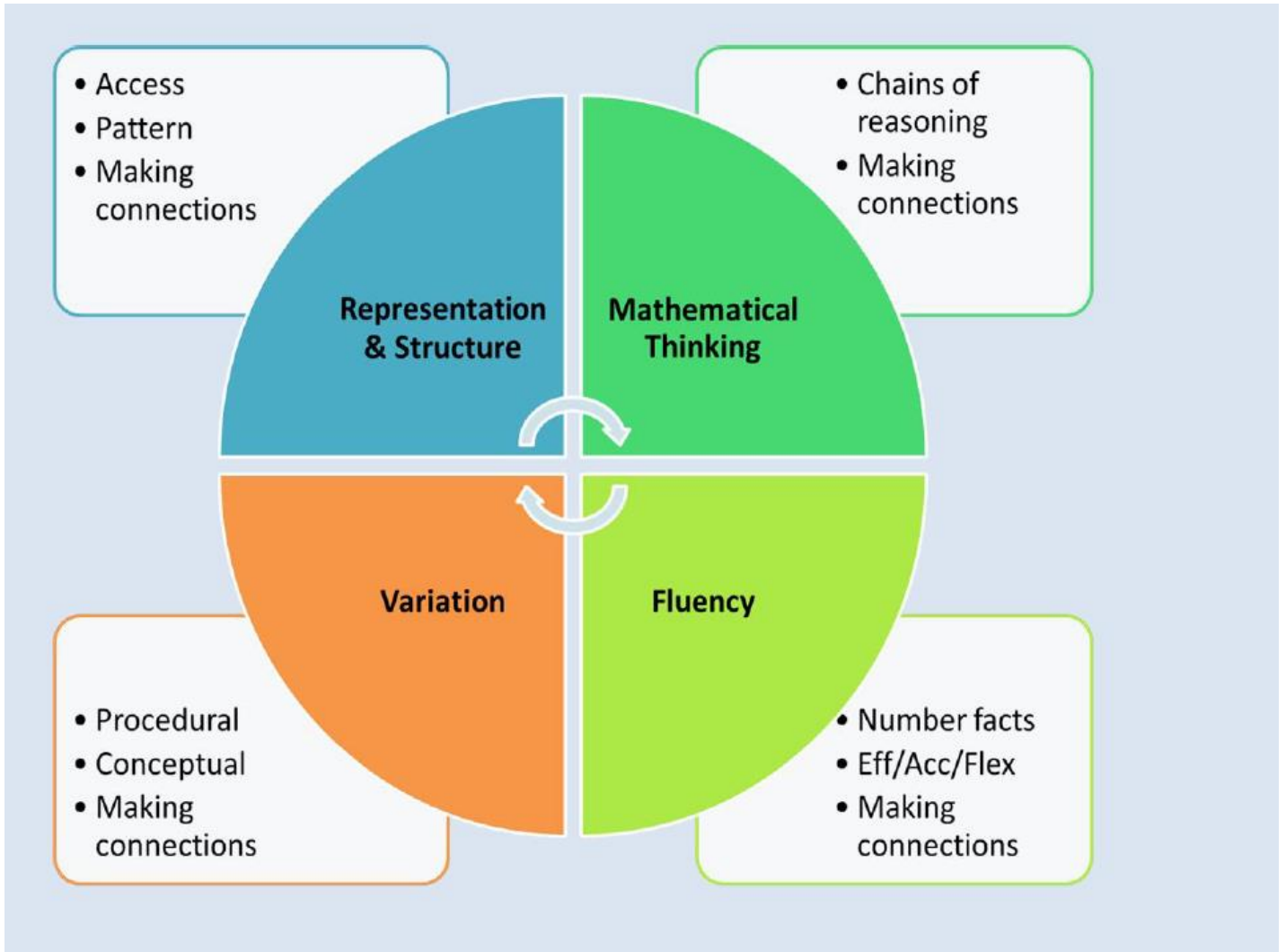
There is also an emphasis placed on instant recall of number bonds and times tables. These need to be mastered to aid with calculations and more challenging problems in readiness for the Multiplication Test at the end of Year 4.

This document outlines the progression of different calculation strategies that could be taught and used from Reception – Year 6, in line with the requirements of the 2014 Primary National Curriculum.

This guidance is to make teachers and parent/carers aware of the progression of strategies that pupils are formally taught that will support them to perform mental and written calculations. In addition, it will support teachers in identifying appropriate pictorial representations and concrete materials to help develop understanding. We have assigned objectives to year groups based upon National Curriculum expectations. However, it is important to remember that it may sometimes be necessary to revisit strategies from previous year groups if children are working below age related expectations.

This guidance only details the strategies; teachers must plan opportunities for pupils to apply these. Concrete materials shown here are for exemplification; there are many other resources which can be used to aid pupil understanding.

This calculation progression document is based on key mastery principles as outlined in the diagram below:



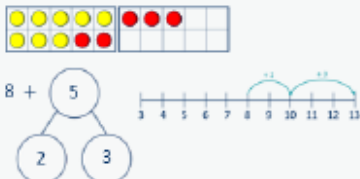
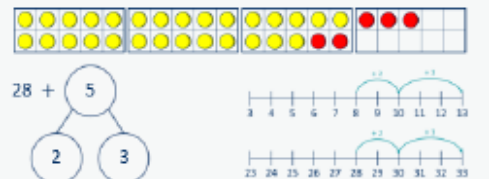
Guidance

The calculation policy is divided into four sections: addition, subtraction, multiplication and division. At the start of each section, you will find an overview of the progression of skills. Calculations involving decimal numbers and fractions are included.

The calculation policy follows the same concrete, pictorial, abstract approach as our main schemes of learning. Where appropriate, sentence stems and key questions are included alongside the key representations.

Where skills are divided into more than one section across the page, there is a progression in the level of difficulty from left to right.

For example, when adding across a 10, children need to be able to add across 10 itself, before making links with related facts.

Add across a 10 Partition the number you are adding to make a full ten.	... can be partitioned into ... and ...  $8 + 5$	I add ... to get to ... then I add ... $8 + 5 = 13$ $28 + 5 = 33$  $28 + 5$
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Progression of skills - Addition




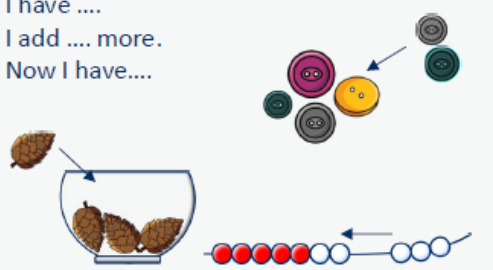
Year group	Skill
Nursery	<ul style="list-style-type: none">• Subitise to 3• Count how many• Make numbers to 5• Add 1 more (through songs and rhymes)
Reception	<ul style="list-style-type: none">• Conceptually subitise to 5• 1 more• Notice the composition of numbers within 10• Combine 2 groups• Add more
Year 1	<ul style="list-style-type: none">• Add together• Add more• Bonds within 10• Related facts within 20• Missing numbers
Year 2	<ul style="list-style-type: none">• Add 1s to any number (related facts)• Add three 1-digit numbers• Add across a 10• Add multiples of 10• Add 10s to any number• Add two 2-digit numbers (not across a ten)• Add two 2-digit numbers (across a ten)• Missing numbers
Year 3	<ul style="list-style-type: none">• Add 1s, 10s and 100s to a 3-digit number• Add two numbers (no exchange)• Add two numbers across a 10 or 100• Complements to 100• Add fractions with the same denominator within 1 whole• Calculate the duration of events


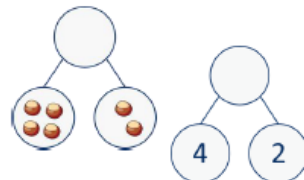
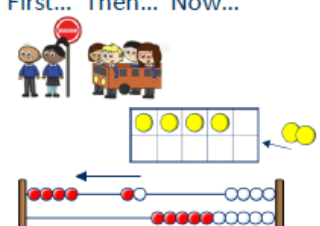
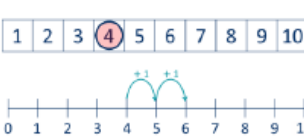
Year 4	<ul style="list-style-type: none"> • Add 1s, 10s and 100s to a 4-digit number • Add up to two 4-digit numbers • Add decimal numbers in the context of money • Add fractions and mixed numbers with the same denominator beyond 1 whole
Year 5	<ul style="list-style-type: none"> • Add using mental strategies • Add whole numbers with more than 4 digits • Add decimals with up to 2 decimal places • Complements to 1 • Add fractions with denominators that are a multiple of one another
Year 6	<ul style="list-style-type: none"> • Add integers up to 10 million • Add decimals with up to 3 decimal places • Order of operations • Negative numbers • Add fractions

Addition

Nursery	<ul style="list-style-type: none"> • Begin to have an understanding of numbers to 5 • We recommend focusing on noticing and representing small quantities, perceptual subitising and counting. 	
Progression of skills	Key representations	
Subitise to 3 Instantly see how many.	How many do you see?	
Count how many Begin to count objects using 1-1 correspondence.	How many are there? 	Count out ... from a larger group. E.g. Collect 3 beanbags for a game.
Make numbers to 5 Start by showing 1, 2 and 3 using fingers.	Show me...	Begin to link numerals to quantities.
Add 1 more Through stories, songs and rhymes.	How many do I have now?	

Reception	<ul style="list-style-type: none"> • Have a deep understanding of numbers to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts. 	
Progression of skills	Key representations	
Conceptually subitise to 5 Notice the parts that make up the whole.	What do you see? How do you see it?	
1 more Continue to link to stories, songs and rhymes.	1 more than ... is ...	
Notice the composition of numbers within 10 Link to stories, songs and rhymes.	How many...? How many...? How many altogether?	How many ways can you make...?

Progression of skills	Key representations	
Combine 2 groups 2 groups are combined to find the total.	There are There are There are altogether.  and make 
Add more A quantity is increased.	First... Then.... Now.... 	I have I add more. Now I have.... 

Year 1	<ul style="list-style-type: none"> Read, write and interpret mathematical statements involving addition (+) and equals (=) signs. Represent and use number bonds within 20 Add 1-digit and 2-digit numbers to 20, including zero. Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as $7 = \square + 2$ 		
Progression of skills	Key representations		
Add together (aggregation) 2 quantities are combined to find the total.	There are ... There are ... There are ... altogether. 	... is a part. ... is a part. ... is the whole. 	... plus ... is equal to is equal to ... + ... $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$
Add more (augmentation) A quantity is increased.	First... Then... Now.... 	I start at ... I jump on ... I land on ... 	... plus ... is equal to is equal to ... + ... $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$

Progression of skills	Key representations		
Bonds within 10 Include bonds for each number within 10 Encourage children to notice patterns.	... is made of ... and and ... make can be partitioned into ... and plus ... is equal to ... $6 + 0 = 6$ $5 + 1 = 6$ $4 + 2 = 6$ $3 + 3 = 6$ $2 + 4 = 6$ $1 + 5 = 6$ $0 + 6 = 6$
Related facts within 20 Make links to known facts.	I know that ... and ... = ... so ... and ... = more than ... is ... so ... more than ... is ... 	What patterns do you notice? $5 + 2 = 7$ $15 + 2 = 17$ $7 = 5 + 2$ $17 = 15 + 2$
Missing numbers Make links to known facts.	How many more do you need to make ...? 	If ... is the whole and ... is a part, the other part must be... 	... plus ... is equal to ... $2 + \square = 6$ $6 = 2 + \square$

Year 2	<ul style="list-style-type: none"> Recall and use addition facts to 20 fluently, and derive and use related facts up to 100 Add numbers using concrete objects, pictorial representations, and mentally, including: <ul style="list-style-type: none"> a two-digit number and 1s a two-digit number and 10s 2 two-digit numbers adding 3 one-digit numbers Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. 		
Progression of skills	Key representations		
Add ones to any number (related facts) Make links to known facts.	I know that ... and ... = ... so ... and ... = more than ... is ... so ... more than ... is ... 	What do you notice? Can you continue the pattern? $5 + 2 = 7$ $15 + 2 = 17$ $25 + 2 = 27...$
Add three 1-digit numbers Prompt children to understand that addition can be done in any order and to make links to known facts.	... and ... are a bond to 10 $10 + \dots = \dots$ 	Double ... + ... = ... 	What do you notice? Which addition is the easiest to calculate? $8 + 9 + 1 =$ $8 + 1 + 9 =$ $9 + 1 + 8 =$

Year 3	<ul style="list-style-type: none"> Add numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. Add numbers with up to three digits, using formal written methods of columnar addition. Add fractions with the same denominator within 1 whole. Calculate the time taken by particular events or tasks.
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Progression of skills	Key representations
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Add 1s, 10s or 100s to a 3-digit number	<p>The ones/tens/hundreds column will increase by ...</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr> <tr><td></td><td></td><td></td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th>H</th><th>T</th><th>O</th></tr> <tr><td></td><td></td><td></td></tr> </table>	Hundreds	Tens	Ones				H	T	O				<p>What patterns do you notice?</p> $235 + 3 =$ $235 + 30 =$ $235 + 300 =$ $111 + \square = 118$ $604 + 20 =$ $604 + 50 =$ $604 + 90 =$ $111 + \square = 181$ $111 + \square = 811$
Hundreds	Tens	Ones												
H	T	O												

Add two numbers (no exchange)	<p>... ones + ... ones = ... ones ... tens + ... tens = ... tens ... hundreds + ... hundreds = ... hundreds</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th colspan="2">?</th></tr> <tr><td>345</td><td>432</td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> </table> <table border="1" style="display: inline-table;"> <tr><th>H</th><th>T</th><th>O</th></tr> <tr><td>3</td><td>4</td><td>5</td></tr> <tr><td>+</td><td>4</td><td>3</td></tr> <tr><td colspan="3">-----</td></tr> <tr><td></td><td></td><td></td></tr> </table>	?		345	432	Hundreds	Tens	Ones							H	T	O	3	4	5	+	4	3	-----					
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Progression of skills	Key representations
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Add two numbers across a 10 or 100	<p>There are ... ones, so I do/do not need to make an exchange. There are ... tens, so I do/do not need to make an exchange. ... ones = ... ten and ... ones. ... tens = ... hundred and ... tens.</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th colspan="2">?</th></tr> <tr><td>255</td><td>54</td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th>H</th><th>T</th><th>O</th></tr> <tr><td>2</td><td>5</td><td>5</td></tr> <tr><td>+</td><td>5</td><td>4</td></tr> <tr><td colspan="3">-----</td></tr> <tr><td></td><td></td><td></td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> </table> <table border="1" style="display: inline-table;"> <tr><th>H</th><th>T</th><th>O</th></tr> <tr><td>4</td><td>6</td><td>6</td></tr> <tr><td>+</td><td>3</td><td>5</td></tr> <tr><td colspan="3">-----</td></tr> <tr><td>8</td><td>1</td><td>9</td></tr> </table>	?		255	54	H	T	O	2	5	5	+	5	4	-----						Hundreds	Tens	Ones							H	T	O	4	6	6	+	3	5	-----			8	1	9
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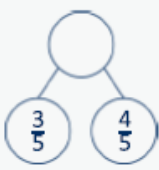
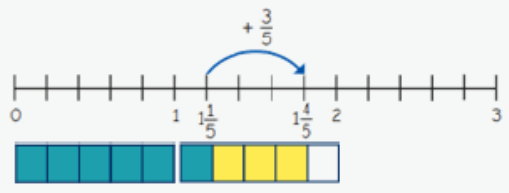
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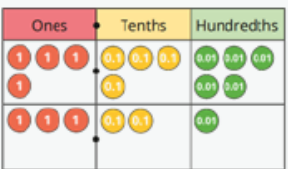
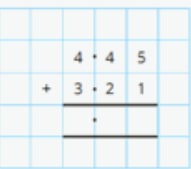
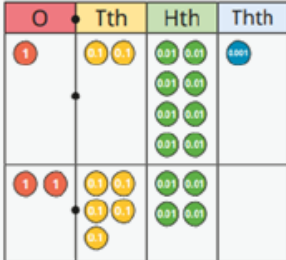
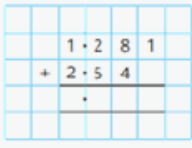
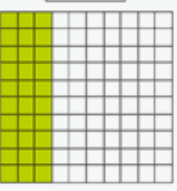
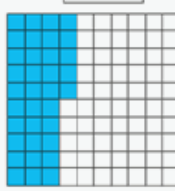
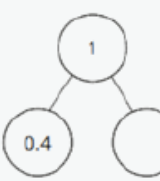

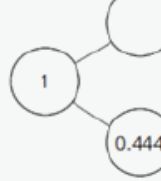
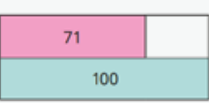
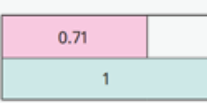
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Complements to 100	<p>... plus ... is equal to 100</p> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><th colspan="2">100</th></tr> <tr><td>38</td><td>?</td></tr> </table> <p>I add ... to get to the next 10, then ... to get to 100</p> $38 + 62 = 100$ $62 + 38 = 100$ $100 = 38 + 62$ $100 = 62 + 38$	100		38	?
100					
38	?				

Progression of skills	Key representations
<p>Add fractions with the same denominator within 1 whole</p> <p>Make links with known facts.</p>	<p>When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths</p> <p>From ... to ... o'clock is ... minutes. From ... o'clock to ... is ... minutes. The total time taken is ... minutes.</p>
<p>Calculate the duration of events</p> <p>Find durations of time between a given start and end point. Children will need to calculate complements to 60</p>	

Year 4	<ul style="list-style-type: none"> Add numbers with up to 4 digits using a formal written method. Solve simple measure and money problems involving fractions and decimals to 2 decimal places. Add fractions with the same denominator. 																								
Progression of skills	Key representations																								
<p>Add 1s, 10s and 100s to a 4-digit number</p> <p>Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.</p>	<p>The ones/tens/hundreds/thousands column will increase by ...</p> <table border="1"> <thead> <tr> <th>Thousands</th> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td>1,000 1,000 1,000</td> <td>100 100 100 100</td> <td>10 10</td> <td>1 1 1 1 1</td> </tr> </tbody> </table> <p>3,425 + 3 = 3,425 + 300 = 3,425 + 30 = 3,425 + 3,000 =</p> <p>What patterns do you notice?</p> <p>2,350 + 3 = 2,350 + 30 = 2,350 + 300 = 2,350 + 3,000 =</p> <p>6,040 + 200 = 2,211 + <input type="text"/> = 2,251 6,040 + 500 = 2,211 + <input type="text"/> = 2,215 6,040 + 900 = 2,211 + <input type="text"/> = 2,511</p>	Thousands	Hundreds	Tens	Ones	1,000 1,000 1,000	100 100 100 100	10 10	1 1 1 1 1																
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1,000 1,000 1,000	100 100 100 100	10 10	1 1 1 1 1																						
<p>Add up to two 4-digit numbers</p> <p>Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<p>There are ... ones/tens/hundreds so I do/do not need to make an exchange.</p> <p>I can exchange 10 ... for 1 ...</p> <table border="1"> <thead> <tr> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>4</td> <td>6</td> <td>7</td> <td>3</td> </tr> <tr> <td>+</td> <td>1</td> <td>5</td> <td>18</td> </tr> <tr> <td colspan="4"><hr/></td> </tr> <tr> <td>6</td> <td>1</td> <td>9</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td></td> <td></td> </tr> </tbody> </table>	Th	H	T	O	4	6	7	3	+	1	5	18	<hr/>				6	1	9	1	1	1		
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Progression of skills	Key representations	
<p>Add decimal numbers in the context of money</p> <p>Emphasis on partitioning and use of number lines rather than formal written calculations.</p>	<p>... pence + ... pence = ... pence ... pounds + ... pounds = ... pounds</p>  <p>$45p + 25p = 70p$ $£2 + £3 = £5$ $£5 + 70p = £5.70$</p>	<p>£3.25 can be partitioned into £3 + 20p + 5p</p> 
<p>Add fractions and mixed numbers with the same denominator beyond 1 whole</p>	<p>When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths</p>  <p>$\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1\frac{2}{5}$</p> 	

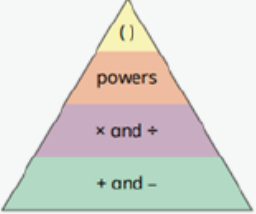
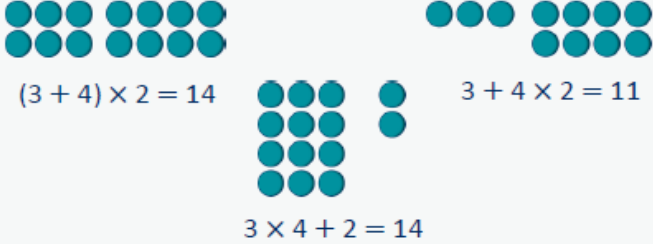
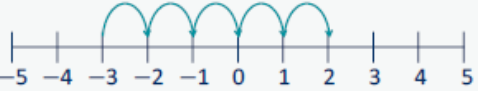
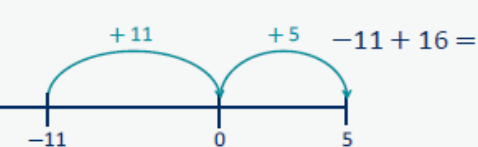
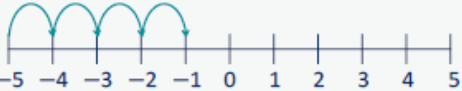
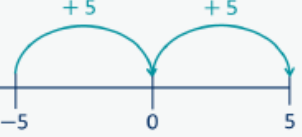
Progression of skills	Key representations	
<p>Add decimals with up to 2 decimal places</p> <p>Progress from the same number of decimal places to a different number of decimal places, and from no exchange to exchange.</p>	<p>I do/do not need to make an exchange because ... I can exchange 10 ... for 1 ...</p>  	 
<p>Complements to 1</p> <p>Pairs of numbers with up to 3 decimal places which total 1</p> <p>Encourage children to make links with bonds to 10 and complements to 100 and 1,000</p>	<p>$0.3 + \square = 1$ $0.35 + \square = 1$</p>      <p>$4 + 6 = 10$ $0.4 + 0.6 = 1$ $44 + 56 = 100$ $0.44 + 0.56 = 1$ $444 + 556 = 1,000$ $0.444 + 0.556 = 1$</p>  	

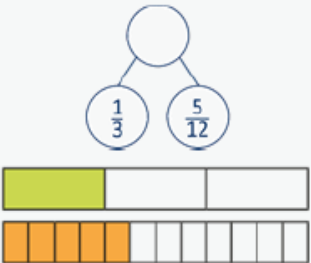
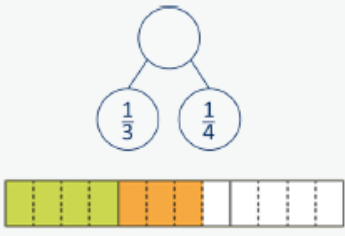
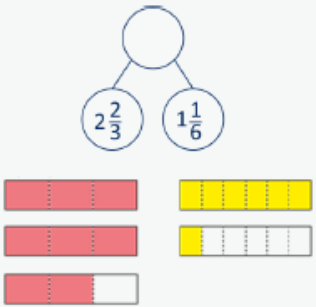
Progression of skills	Key representations
<p>Add fractions with denominators that are a multiple of one another</p> <p>Encourage children to convert fractions to the same denominator before adding.</p> <p>Progress from adding fractions within 1 whole to adding fractions beyond 1 whole.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> $\frac{1}{2} + \frac{1}{8} = \frac{4}{8} + \frac{1}{8} = \frac{5}{8}$ </div> <div style="text-align: center;"> $\frac{3}{4} + \frac{5}{8} = \frac{6}{8} + \frac{5}{8} = \frac{11}{8} = 1\frac{3}{8}$ </div> </div>

Year 6	<ul style="list-style-type: none"> • Add larger numbers, using the formal written method of columnar addition. • Use their knowledge of the order of operations to carry out calculations involving the 4 operations. • Calculate intervals across zero. • Add fractions with different denominators and mixed numbers, using the concept of equivalent fractions.
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Progression of skills	Key representations																																																																														
<p>Add integers up to 10 million</p> <p>Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td>3</td><td>4</td><td>6</td><td>2</td><td>2</td><td>1</td></tr> <tr><td></td><td></td><td>+</td><td>1</td><td>8</td><td>4</td><td>3</td><td>2</td></tr> <tr><td></td><td></td><td></td><td>5</td><td>3</td><td>0</td><td>5</td><td>4</td></tr> <tr><td></td><td></td><td></td><td>1</td><td>1</td><td></td><td></td><td></td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td colspan="3" style="background-color: #f8d7da;">?</td></tr> <tr><td>2,354</td><td>750</td><td>1,500</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td>8</td><td>1</td><td></td><td>8</td><td>5</td><td></td></tr> <tr><td></td><td></td><td>+</td><td></td><td></td><td>0</td><td>6</td><td></td></tr> <tr><td></td><td></td><td></td><td>9</td><td>9</td><td>5</td><td></td><td>8</td></tr> </table> </div>											3	4	6	2	2	1			+	1	8	4	3	2				5	3	0	5	4				1	1				?			2,354	750	1,500											8	1		8	5				+			0	6					9	9	5		8
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<p>Add decimals with up to 3 decimal places</p> <p>Progress to numbers with digits in different place value columns.</p> <p>Encourage children to check that they have lined up the columns correctly.</p>	<p>I do/do not need to make an exchange because ...</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th>0</th><th>Tth</th><th>Hth</th><th>Thth</th></tr> <tr><td>1</td><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>0</td><td>0</td></tr> <tr><td>5</td><td>2</td><td>6</td><td>2</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td>3</td><td>1</td><td>0</td><td>8</td></tr> <tr><td></td><td></td><td>+</td><td>2</td><td>1</td><td>5</td></tr> <tr><td></td><td></td><td></td><td>5</td><td>2</td><td>6</td></tr> <tr><td></td><td></td><td></td><td></td><td></td><td>2</td></tr> <tr><td></td><td></td><td></td><td></td><td></td><td>1</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td><td>1</td><td>5</td><td>0</td><td>2</td><td>7</td></tr> <tr><td></td><td></td><td></td><td>+</td><td>9</td><td>5</td><td>8</td><td></td></tr> <tr><td></td><td></td><td></td><td></td><td>2</td><td>4</td><td>6</td><td>0</td></tr> <tr><td></td><td></td><td></td><td></td><td>1</td><td>1</td><td></td><td></td></tr> </table> </div>	0	Tth	Hth	Thth	1	1	0	0	1	1	0	0	1	1	0	0	5	2	6	2									3	1	0	8			+	2	1	5				5	2	6						2						1												1	5	0	2	7				+	9	5	8						2	4	6	0					1	1		
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Progression of skills	Key representations	
<p>Order of operations</p> <p>Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets are shown and the operations have the same priority, work left to right.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p>  	
<p>Negative numbers</p> <p>Children add to negative numbers and carry out calculations which cross 0</p>	<p>... plus ... is equal to ...</p> <p>$-3 + 5 = 2$</p>  <p>$-11 + 16 = 5$</p> 	 <p>The difference between -5 and -1 is 4</p>  <p>The difference between -5 and 5 is 10</p>


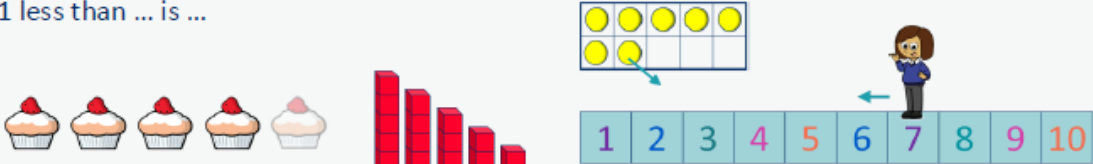


Progression of skills	Key representations		
<p>Add fractions</p> <p>Convert fractions to the same denominator before adding. Progress from fractions where one denominator is a multiple of the other, to any fractions and then to mixed numbers.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by ...</p> 	<p>The lowest common multiple of ... and ... is ...</p>  <p>$\frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12} = \frac{7}{12}$</p>	<p>...is made up of ... wholes and ...</p> 



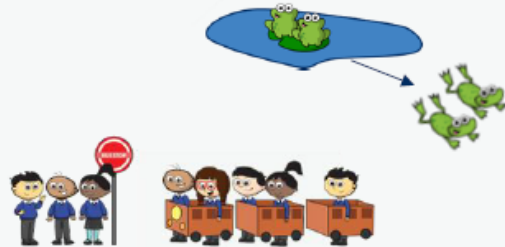
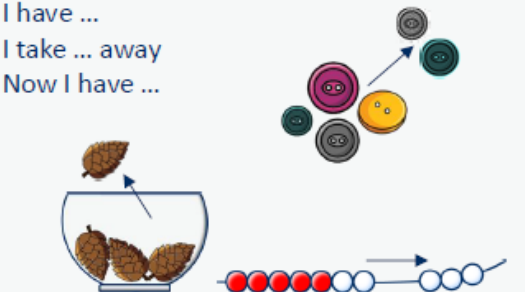
Progression in skills – Subtraction

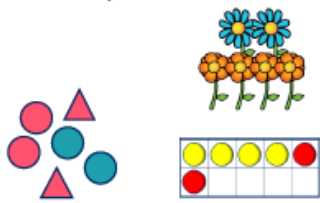
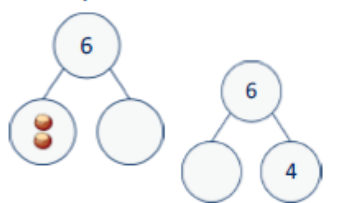
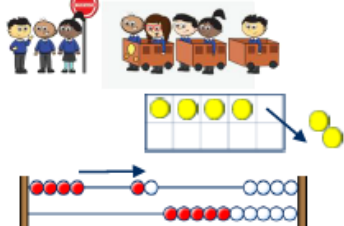
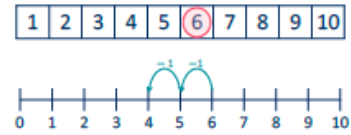
Year group	Skill
Nursery	<ul style="list-style-type: none">• Subitise to 3• Count how many• Make numbers to 5• Take 1 away (through songs and rhymes)
Reception	<ul style="list-style-type: none">• Conceptually subitise to 5• 1 less• Notice the composition of numbers within 10• Partition• Take away
Year 1	<ul style="list-style-type: none">• Find a part• Take away• Bonds within 10• Related facts within 20• Missing numbers
Year 2	<ul style="list-style-type: none">• Subtract 1s from any number (related facts)• Subtract across a 10• Subtract multiples of 10• Subtract 10s from any number• Subtract two 2-digit numbers (not across a ten)• Subtract two 2-digit numbers (across a ten)• Missing numbers
Year 3	<ul style="list-style-type: none">• Subtract 1s, 10s and 100s from a 3-digit number• Subtract two numbers (no exchange)• Subtract two numbers across a 10 or 100• Complements to 100• Subtract fractions with the same denominator within 1 whole


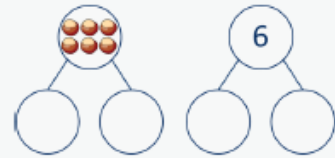
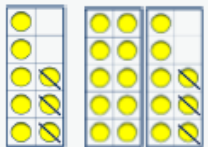
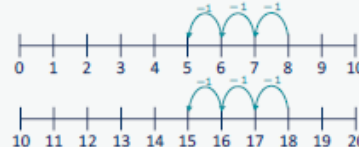

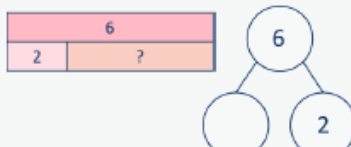

Year 4	<ul style="list-style-type: none"> Subtract 1s, 10s, 100s and 1,000s from a 4-digit number Subtract up to two 4-digit numbers Subtract decimal numbers in the context of money Subtract fractions and mixed numbers with the same denominator
Year 5	<ul style="list-style-type: none"> Subtract whole numbers with more than 4 digits Subtract using mental strategies Subtract decimals with up to 2 decimal places Complements to 1 Subtract fractions with denominators that are a multiple of one another
Year 6	<ul style="list-style-type: none"> Subtract integers up to 10 million Subtract decimals with up to 3 decimal places Order of operations Negative numbers Subtract fractions

Nursery	<ul style="list-style-type: none"> Begin to have an understanding of numbers to 5 We recommend focusing on noticing and representing small quantities, perceptual subitising and counting. 	
Progression of skills	Key representations	
Subitise to 3 Instantly see how many.	How many do you see?        	
Count how many Begin to count objects using 1-1 correspondence.	How many are there? 1 2 3 4 5 	Count out ... from a larger group. E.g. Collect a cup for everyone at the table. 
Make numbers to 5 Start by showing 1, 2 and 3 using fingers.	Show me...  	Begin to link numerals to quantities. 
Take 1 away Through stories, songs and rhymes.	How many do we have now? 	

<p>Reception</p>	<ul style="list-style-type: none"> • Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (and some subtraction facts) and some number bonds to 10, including double facts. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Conceptually subitise to 5</p> <p>Notice the parts that make up the whole.</p>	<p>What do you see? How do you see it?</p> 	
<p>1 less</p> <p>Continue to link to stories, songs and rhymes.</p>	<p>1 less than ... is ...</p> 	
<p>Notice the composition of numbers within 10</p> <p>Link to stories, songs and rhymes.</p>	<p>How many...? How many...? How many altogether?</p> 	<p>How many ways can you make...?</p> 


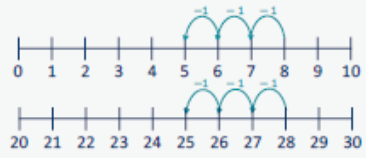
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Partition</p> <p>Using objects, explore different ways to partition a number into 2 or more parts.</p>	<p>There are ... altogether. I can see ... here and ... there.</p>  <p>... and ... make ...</p> 	
<p>Take away</p> <p>A quantity is reduced.</p>	<p>First... Then... Now...</p>  <p>I have ... I take ... away Now I have ...</p> 	

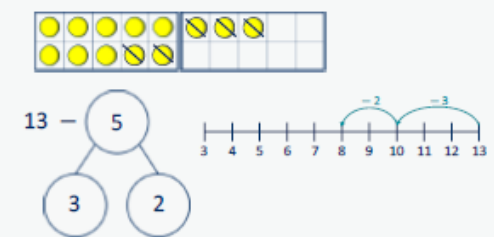
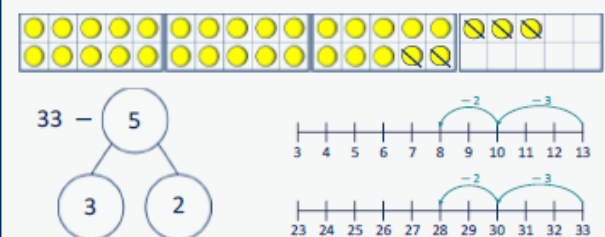
<p>Year 1</p>	<ul style="list-style-type: none"> • Read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs. • Represent and use number bonds and related subtraction facts within 20 • Subtract one-digit and two-digit numbers to 20, including zero. • Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$ 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Find a part</p> <p>Link to number bonds and known facts. E.g. $2 + 4 = 6$ so if 6 is the whole and 4 is a part, the other part must be 2</p>	<p>There are ... in total. ... are ... How many are not ...?</p> 	<p>... is the whole. ... is a part. ... is a part.</p> 	<p>... subtract ... is equal to is equal to ... – ...</p> $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
<p>Take away</p> <p>A quantity is decreased.</p>	<p>First... Then... Now...</p> 	<p>I start at ... I jump back ... I land on ...</p> 	<p>... minus ... is equal to is equal to ... – ...</p> $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$

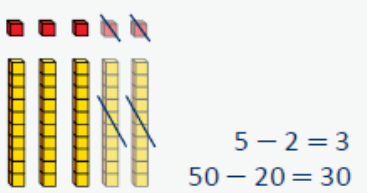
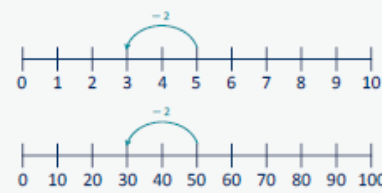

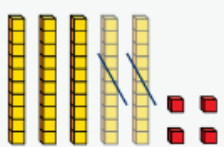
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Bonds within 10</p> <p>Focus on subtraction facts.</p> <p>Encourage children to notice patterns.</p>	<p>... is made of ... and and ... make ...</p> 	<p>... can be partitioned into ... and ...</p> 	<p>... minus ... is equal to ...</p> $6 - 0 = 6$ $6 - 1 = 5$ $6 - 2 = 4$ $6 - 3 = 3$ $6 - 4 = 2$ $6 - 5 = 1$ $6 - 6 = 0$
<p>Related facts within 20</p> <p>Make links to known facts.</p>	<p>I know that ... minus ... = ... so ... minus ... = ...</p> 	<p>... less than ... is ... so ... less than ... is ...</p> 	<p>What patterns do you notice?</p> $8 - 3 = 5$ $18 - 3 = 15$ $5 = 8 - 3$ $15 = 18 - 3$
<p>Missing numbers</p> <p>Make links to known facts.</p>	<p>How many do you need to subtract to make ...?</p> 	<p>If ... is the whole and ... is a part, the other part must be...</p> 	<p>... minus ... is equal to ...</p> $6 - \square = 2$ $2 = 6 - \square$ 

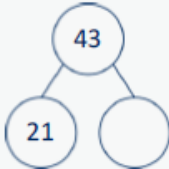
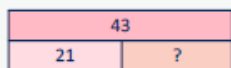
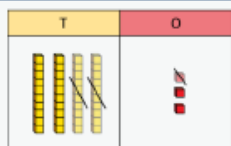
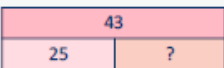
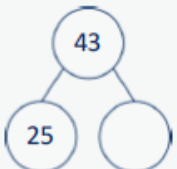
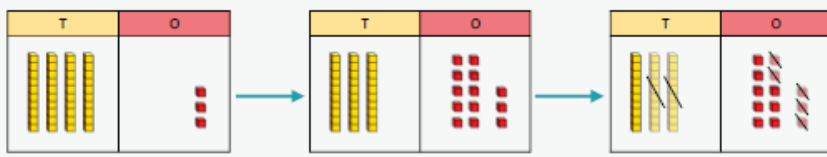
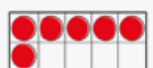
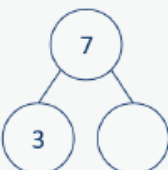
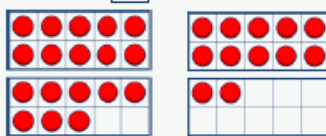
	<ul style="list-style-type: none"> Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100 Subtract numbers using concrete objects, pictorial representations, and mentally, including: <ul style="list-style-type: none"> a two-digit number and 1s a two-digit number and 10s 2 two-digit numbers Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.
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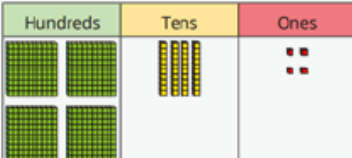
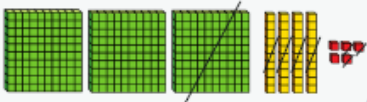
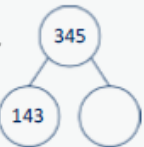
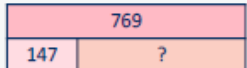


Progression of skills	Key representations
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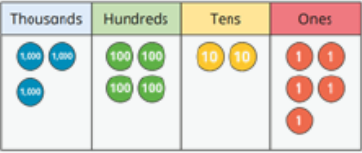
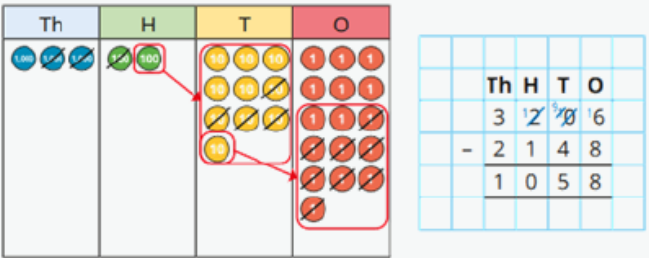
Subtract ones from any number (related facts) Make links to known facts.	I know that ... minus ... = ... so ... minus ... = ... 	... less than ... is ... so ... less than ... is ... 	What do you notice? Can you continue the pattern? $8 - 3 = 5$ $18 - 3 = 15$ $28 - 3 = 25...$
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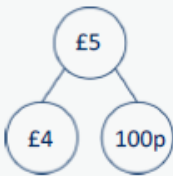

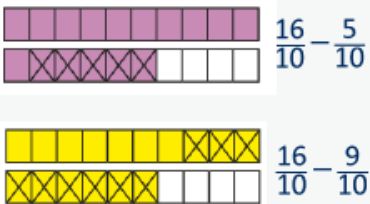
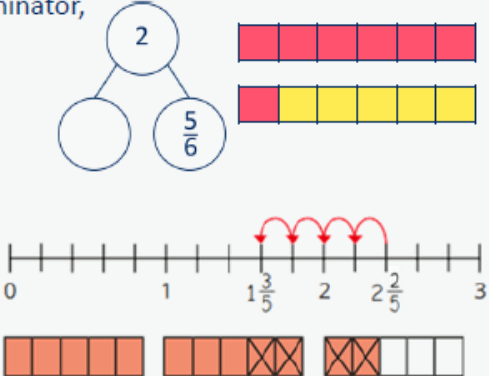
Subtract across a 10 Partition the number being subtracted to bridge through a ten.	... can be partitioned into ... and ... 	Make links with related facts. 
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Progression of skills	Key representations																																																														
Subtract multiples of 10 Make links to known facts within ten.	... ones - ... ones = ... ones so ... tens - ... tens = ... tens 	What is the same? What is different?   <table border="1" data-bbox="1284 1657 1508 1780"> <tr><td colspan="2">5</td></tr> <tr><td>2</td><td>?</td></tr> <tr><td colspan="2">50</td></tr> <tr><td>20</td><td>?</td></tr> </table>	5		2	?	50		20	?																																																					
5																																																															
2	?																																																														
50																																																															
20	?																																																														
Subtract 10s from any number Make links to known facts.	... tens - ... tens = ... tens ... tens and ... ones = ... 	To subtract ... I need to subtract 10 ... times. <table border="1" data-bbox="837 1937 1173 2116"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> <tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	I know that ... minus ... = ... so ... minus ... = ... $50 - 20 = 30$ $54 - 20 = 34$
1	2	3	4	5	6	7	8	9	10																																																						
11	12	13	14	15	16	17	18	19	20																																																						
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51	52	53	54	55	56	57	58	59	60																																																						

Progression of skills	Key representations		
Subtract two 2-digit numbers (not across a ten)	\dots ones $- \dots$ ones = \dots ones \dots tens $- \dots$ tens = \dots tens  	 $3 \text{ ones} - 1 \text{ one} = 2 \text{ ones}$ $4 \text{ tens} - 2 \text{ tens} = 2 \text{ tens}$ $2 \text{ tens and } 2 \text{ ones} = 22$	
Subtract two 2-digit numbers (across a ten) Begin to exchange 1 ten for 10 ones.	I need to make an exchange because I do not have enough ones to subtract \dots ones.  	 $3 \text{ ones} - 5 \text{ ones}$ (I need to exchange 1 ten for 10 ones) $13 \text{ ones} - 5 \text{ ones} = 8 \text{ ones}$ $3 \text{ tens} - 2 \text{ tens} = 1 \text{ ten}$ $1 \text{ ten and } 8 \text{ ones} = 18$	
Missing numbers Solve missing number problems and use the inverse to check.	How many do you need to subtract to make \dots ?  $10 - \square = 6$ $6 + \square = 10$	If \dots is a whole and \dots is a part, then \dots is the other part. $7 - 3 = \square$ $\square + 3 = 7$ 	\dots can be partitioned into \dots and \dots $18 - \square = 12 + 2$ 

Year 3	<ul style="list-style-type: none"> Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. Subtract numbers with up to three digits, using formal written methods. Subtract fractions with the same denominator within 1 whole. 	
Progression of skills	Key representations	
Subtract 1s, 10s and 100s from a 3-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds column will decrease by ...  $444 - 2 =$ $444 - 20 =$ $444 - 200 =$	What patterns do you notice? $235 - 3 =$ $235 - 30 =$ $235 - 300 =$ $118 - \square = 111$ $624 - 20 =$ $181 - \square = 111$ $654 - 50 =$ $811 - \square = 111$
Subtract two numbers (no exchange) Mental strategies and introduction of formal written method.	\dots ones $- \dots$ ones = \dots ones \dots tens $- \dots$ tens = \dots tens \dots hundreds $- \dots$ hundreds = \dots hundreds  	  

Year 4	<ul style="list-style-type: none"> Subtract numbers with up to 4 digits using a formal written method. Solve simple measure and money problems involving fractions and decimals to 2 decimal places. Subtract fractions with the same denominator. 	
Progression of skills	Key representations	
Subtract 1s, 10s, 100s and 1,000s from a 4-digit number Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.	The ones/tens/hundreds/thousands column will decrease by ...  $3,425 - 2 =$ $3,425 - 200 =$ $3,425 - 20 =$ $3,425 - 2,000 =$	What patterns do you notice? $4,356 - 3 =$ $4,356 - 30 =$ $4,356 - 300 =$ $4,356 - 3,000 =$ $6,940 - 200 =$ $4,433 - \square = 4,430$ $6,940 - 300 =$ $4,433 - \square = 4,033$ $6,940 - 400 =$ $4,433 - \square = 4,403$
Subtract up to two 4-digit numbers Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.	I need to subtract... ones/tens/hundreds. I do/do not need to make an exchange. I can exchange 1... for 10... 	

Progression of skills	Key representations	
Subtract decimal numbers in the context of money Emphasis here is on partitioning and use of number lines rather than formal written calculations.	I can partition £... into £... and 100p $£... - £... = £...$ $100p - ...p = ...p$ $£5 - £3.26$ $£4 - £3 = £1$ $100p - 26p = 74p$ $£5 - £3.26 = £1.74$ 	$£3.26$ can be partitioned into $£3 + 20p + 6p$ 
Subtract fractions and mixed numbers with the same denominator Include subtracting fractions from wholes.	When subtracting fractions with the same denominator, I only subtract the numerator. $... \text{ tenths} - ... \text{ tenths} = ... \text{ tenths}$  	

Year 5	<ul style="list-style-type: none"> Subtract whole numbers with more than 4 digits. Subtract numbers mentally with increasingly large numbers. Subtract decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1 Subtract fractions with the same denominator, and denominators that are multiples of the same number.
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Progression of skills	Key representations
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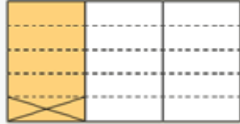

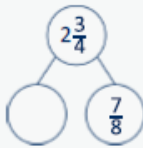
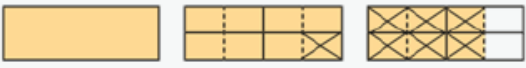
Subtract whole numbers with more than 4 digits	<p>I can exchange 1 ... for 10 ...</p>
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Subtract using mental strategies	<p>To subtract ..., I can subtract ... then add ...</p>
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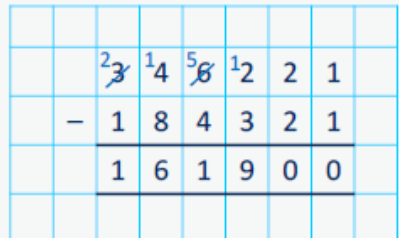
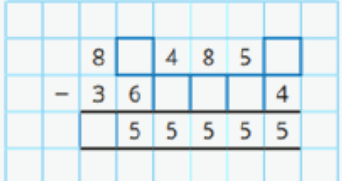
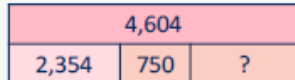
Progression of skills	Key representations
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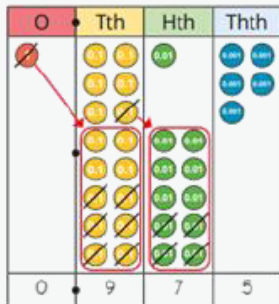
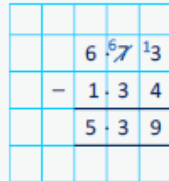
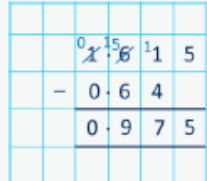
Subtract decimals with up to 2 decimal places	<p>Progress from the same number of decimal places to a different number of decimal places and from no exchange to exchange.</p>
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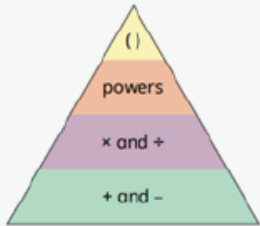







Complements to 1	<p>Encourage children to make links with bonds to 10 and complements to 100 and 1,000 when finding a missing part or subtracting from 1</p>
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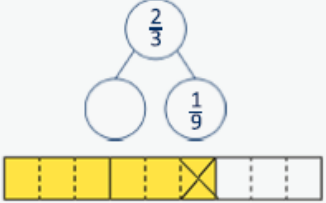
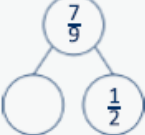
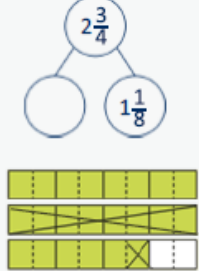
Progression of skills	Key representations
<p>Subtract fractions with denominators that are a multiple of one another</p> <p>Convert fractions to the same denominator before subtracting. Progress from subtracting fractions within 1 whole to subtracting from a mixed number.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.</p>   $\frac{2}{3} - \frac{2}{9} = \frac{6}{9} - \frac{2}{9} = \frac{4}{9}$ $\frac{1}{3} - \frac{1}{15} = \frac{5}{15} - \frac{1}{15} = \frac{4}{15}$  

Year 6	<ul style="list-style-type: none"> Subtract larger numbers, using the formal written methods of columnar subtraction. Use their knowledge of the order of operations to carry out calculations involving the 4 operations. Calculate intervals across zero. Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions.
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Progression of skills	Key representations
<p>Subtract integers up to 10 million</p> <p>Encourage children to estimate and use inverse operations to check answers to calculations.</p>	  

<p>Subtract decimals with up to 3 decimal places</p> <p>Progress from the same number of decimal and whole number places to a different number of decimal and whole number places.</p>	<p>I do/do not need to make an exchange because ...</p>   
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Progression of skills	Key representations	
<p>Order of operations</p> <p>Children learn the order of priority for operations in a calculation. Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  <p>$8 - 2 \times 3 = 2$</p> </div> <div style="text-align: center;">  <p>$(8 - 2) \times 3 = 18$</p> </div> <div style="text-align: center;">  <p>$8 - 2^2 = 4$</p> </div> </div>	
<p>Negative numbers</p> <p>Children subtract from positive and negative numbers and calculate intervals across 0</p>	<p>... minus ... is equal to ...</p> <p style="text-align: right;">$-1 - 4 = -5$</p>  <p style="text-align: right;">$1 - 4 = -3$</p> 	 <p>The difference between -5 and -1 is 4</p>  <p>The difference between 5 and -5 is 10</p>

Progression of skills	Key representations		
<p>Subtract fractions</p> <p>Convert fractions to the same denominator before subtracting. Progress from fractions where one denominator is a multiple of the other, to any fractions and then subtracting from a mixed number.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by...</p> <div style="text-align: center;">  </div> <p style="text-align: center;">$\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$</p>	<p>The lowest common multiple of ... and ... is ...</p> <div style="text-align: center;">  </div> <p style="text-align: center;">$\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$</p>	<p>... is made up of ... wholes and ...</p> <div style="text-align: center;">  </div> <p style="text-align: center;">$2 \frac{3}{4} - 1 \frac{1}{8} = 1 \frac{5}{8}$</p>

Progression of skills – Multiplication

Year group	Skill
Nursery	<ul style="list-style-type: none"> Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)
Reception	<ul style="list-style-type: none"> Double to 10 Make equal groups
Year 1	<ul style="list-style-type: none"> Count in 2s, 5s and 10s Add equal groups Make arrays Make doubles
Year 2	<ul style="list-style-type: none"> Link repeated addition and multiplication Use arrays Double The 2 times-table The 10 times-table The 5 times-table Missing numbers
Year 3	<ul style="list-style-type: none"> The 3 times-table The 4 times-table The 8 times-table Related facts Multiply a 2-digit number by a 1-digit number - no exchange Multiply a 2-digit number by a 1-digit number - with exchange Scaling Correspondence problems

Year 4

- Times-table facts to 12×12
- Multiply by 1 and 0
- Multiply 3 numbers
- Factor pairs
- Multiply by 10 and 100
- Related facts
- Mental strategies
- Multiply a 2 or 3-digit number by a 1-digit number
- Scaling
- Correspondence problems

Year 5

- Multiples and factors
- Square and cube numbers
- Multiply numbers up to 4 digits by a 1-digit number
- Multiply numbers up to 4 digits by a 2-digit number
- Multiply by 10, 100 and 1,000
- Mental strategies
- Multiply fractions by a whole number
- Multiply mixed numbers by a whole number
- Find the whole

Year 6

- Multiply numbers up to 4 digits by a 2-digit number
- Multiply by 10, 100 and 1,000
- Order of operations
- Multiply decimals by integers
- Multiply fractions by fractions
- Find the whole
- Calculations involving ratio

Reception

- Have a deep understanding of number to 10, including the composition of each number.
- Subitise (recognise quantities without counting) up to 5
- Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts.
- Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.

Progression of skills

Key representations

Double to 10

Prompt children to notice that double means twice as many and to notice that there are two equal groups.

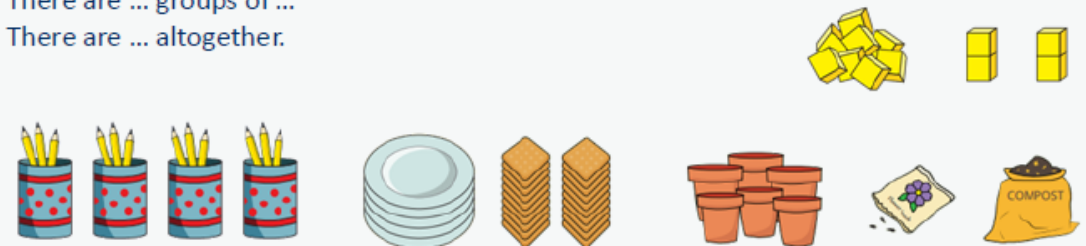
Double ... is ...
... is double ...



Make equal groups

Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.

There are ... groups of ...
There are ... altogether.



Year 1	<ul style="list-style-type: none"> Count in multiples of twos, fives and tens. Solve one-step problems involving multiplication, using concrete objects, pictorial representations and arrays with the support of the teacher.
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Progression of skills	Key representations
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Count in 2s, 5s and 10s

Begin by counting objects that naturally come in 2s, 5s and 10s, for example pairs of socks or fingers.

There are ... equal groups of ...
There are ... altogether.

Continue to colour in ...s
What do you notice?

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

Complete the number track/number line by counting in ...s.

5	10	15	20				
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Add equal groups (repeated addition)

Children should be able to write a repeated addition to represent equal groups and to draw pictures or use objects to represent a repeated addition.

There are ... groups of ...
There are ... altogether.

$10 + 10 + 10 = 30$

$5 + 5 + 5 + 5 = 20$

What is the same? What is different?

$2 + 2 + 2 =$

$5 + 5 + 5 =$

$10 + 10 + 10 =$

Use objects or a drawing to represent the equal groups and find how many in total.